

Comments by Rafael Repullo on

**Risk-taking and Joint  
Liquidity and Capital Regulation**

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# Purpose of paper

- Moral hazard model of a single bank
  - Bank chooses capital, liquidity, and risk
  - Choice of risk is not observed by regulator
  - Depends on capital and liquidity
- Social welfare maximizer regulator
  - Can set minimum capital and liquidity requirements
  - Characterize second-best optimal requirements

# Setup

- Limited liability bank chooses capital, liquidity, and risk at  $t = 0$ 
  - Subject to capital and liquidity requirements
  - Insured deposits
  - Costly capital (more than deposits)
  - Costly liquidity (lower return than risky asset)
- Stochastic deposits withdrawals at  $t = 1$ 
  - Bank is closed if liquidity does not cover withdrawals

# Main results

- Capital and liquidity requirements should be set jointly
  - Unlike in the silo approach of Basel III
- Optimal capital and liquidity requirements depend on
  - Cost of capital and opportunity cost of liquidity
  - Unlike in the statistical/quantitative approach of Basel III
- Differences between capital and liquidity requirements
  - Capital requirements always ameliorate risk-taking
  - Liquidity requirements may or may not do so

# Main comments

- Paper is too long and unnecessarily convoluted
  - Sequential approach to solving maximization problem
  - Why not do it simultaneously?
- Paper considers exogenous deposit withdrawals
  - Appropriate given deposit insurance
  - But not if (part of) the bank's funding is uninsured
- Lender of last resort (LoLR) should be at the core of the paper
  - Do we need liquidity requirements when there is a LoLR?

# What am I going to do?

- Consider a simple version of the model
- Derive three sets of results
  - No regulation (*laissez faire*)
  - Optimal regulation without moral hazard
  - Optimal regulation with moral hazard
- Briefly comment on related work on joint regulation
  - Rochet and Vives (2004) and König (2015)

# **Part 1**

## **A simple version of the model**

# Model setup

- Three dates ( $t = 0, 1, 2$ )
- Balance sheet of the bank at  $t = 0$

Liquidity	→	$l$		$d$	←	Demand deposits
Risky asset	→	$1 - l$		$b$	←	Other deposits
				$k$	←	Capital



# Bank's liabilities

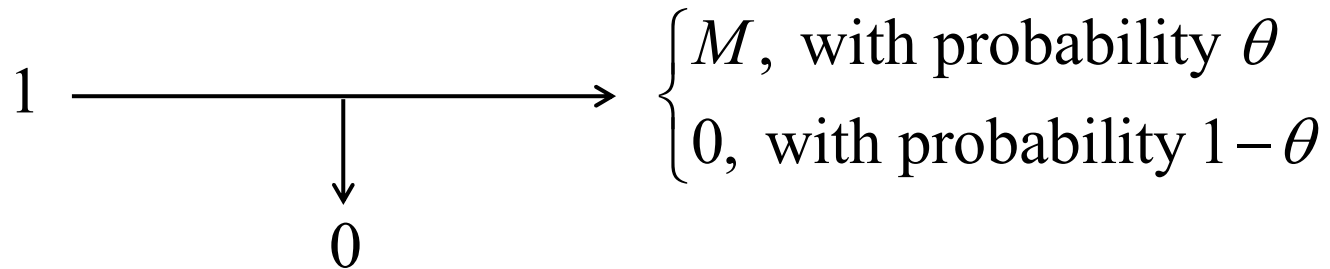
- Fixed demand deposits  $d$ 
  - Interest rate normalized to zero
  - Amount  $\beta$  withdrawn at  $t = 1$
  - Assume uniform distribution in  $[0, d]$
- Variable other deposits  $b$ 
  - Interest rate assumed to be zero
- Variable capital  $k$  (such that  $k + b = 1 - d$ )
  - Cost of capital  $\rho > 0$

# Bank's assets

- Safe asset (liquidity)

→ Interest rate assumed to be zero

- Risky asset



→ Success probability chosen by bank at  $t = 0$  at a cost

$$c(\theta) = \frac{c}{2} \theta^2$$

# Bank's objective function

- Two possible cases

→ If  $\beta > l$  bank is closed and shareholders get zero

→ If  $\beta \leq l$  bank is not closed and shareholders get

$$\begin{aligned} M(1-l) + (l-\beta) - (1-k-\beta) \\ = M(1-l) + l - (1-k), \text{ with prob. } \theta \end{aligned}$$

- Bank expected payoff

$$\pi(k, l, \theta) = [M(1-l) + l - (1-k)]\theta F(l) - \frac{c}{2}\theta^2 - (1+\rho)k$$

# Laissez faire

- First-order conditions

$$\frac{\partial \pi}{\partial k} = \theta F(l) - (1 + \rho) < 0 \rightarrow k^{LF} = 0$$

$$\frac{\partial \pi}{\partial l} = 0 \rightarrow l^{LF} = \frac{M - 1 + k}{2(M - 1)} = \frac{1}{2}$$

$$\frac{\partial \pi}{\partial \theta} = 0 \rightarrow \theta^{LF} = \frac{[(M - 1)(1 - l) + k]F(l)}{c} = \frac{M - 1}{4cd}$$

# Social planner's objective function

- Social planner's expected payoff

$$\omega(k, l, \theta) = M(1-l)\theta F(l) + l - (1-k) - \frac{c}{2}\theta^2 - (1+\rho)k$$

- Two cases

→ First-best: Regulator chooses capital, liquidity, and risk

→ Second-best: Regulator chooses capital and liquidity +

Bank chooses risk

# First-best

- First-order conditions

$$\frac{\partial \omega}{\partial k} = -\rho < 0 \rightarrow k^{FB} = 0$$

$$\frac{\partial \omega}{\partial l} = 0 \rightarrow l^{FB} = \frac{1}{2} + \frac{d}{2M\theta}$$

$$\frac{\partial \omega}{\partial \theta} = 0 \rightarrow \theta^{FB} = \frac{M(1-l)}{cd}$$

# Comparison of first-best with laissez faire

- Numerical example: Let  $M = 2$ ,  $c = 2/3$ , and  $d = 3/4$ 
  - $k^{LF} = k^{FB} = 0$
  - $l^{LF} = 0.50 < 0.75 = l^{FB}$
  - $\theta^{LF} = 0.50 < 0.75 = \theta^{FB}$
- First-best also has zero capital
  - Capital is costly and is not needed to provide incentives
- First-best has more liquidity and less risk than laissez faire

## Second-best: bank's choice of risk

- First-order condition

$$\frac{\partial \pi}{\partial \theta} = 0 \quad \rightarrow \quad \theta = \theta(k, l) = \frac{[(M - 1)(1 - l) + k]l}{cd}$$

- Notice that

$$\frac{\partial \theta}{\partial k} > 0$$

→ Capital requirements always ameliorate risk-taking

$$\frac{\partial \theta}{\partial l} > 0 \quad \text{if and only if} \quad l < \frac{M - 1 + k}{2(M - 1)}$$

→ Liquidity requirements when they are not too large



## Second best

- Social planner's problem

$$\max_{k,l} \omega(k,l,\theta) \text{ subject to } \theta = \theta(k,l)$$

→ First-order conditions

$$\frac{\partial \omega}{\partial k} = -\rho + \left( \frac{M(1-l)l}{d} - c\theta \right) \frac{\partial \theta}{\partial k} = 0$$

$$\frac{\partial \omega}{\partial l} = \frac{M(1-2l)\theta}{d} + 1 + \left( \frac{M(1-l)l}{d} - c\theta \right) \frac{\partial \theta}{\partial l} = 0$$

→ Be careful with corner solutions!

# Comparison of second-best with laissez faire

- Numerical example: Let  $M = 2$ ,  $c = 2/3$ ,  $d = 3/4$ , and  $\rho = 0.1$ 
  - $k^{LF} = 0 < 0.18 = k^{SB}$
  - $l^{LF} = 0.50 < 0.75 = l^{SB}$
  - $\theta^{LF} = 0.50 < 0.65 = \theta^{SB}$
- Second-best has positive level of capital
  - To ameliorate risk-taking incentives
- Second-best has more liquidity and less risk than laissez faire

## Comments on extensions

- Possible liquidation of risky asset at  $t = 1$  at fire sale discount
  - Interesting, but note that discount is exogenous
- Possible interbank market at  $t = 1$ 
  - Interesting, but need to think about withdrawals
  - Are they driven by idiosyncratic or aggregate shocks?
- Possible information-based withdrawals
  - May need a completely different setup

## **Part 2**

### **Related work on joint regulation**

# Introduction

- Change of focus
  - From retail deposits to (informed) wholesale investors
  - From stochastic withdrawals to information-based runs
- Change of modeling approach
  - Global games

## Model setup (i)

- Three dates ( $t = 0, 1, 2$ )
- Continuum of risk-neutral investors
  - Invest  $D$  in the bank at  $t = 0$
  - May withdraw  $DR_D$  at  $t = 1$  or  $t = 2$ , with  $R_D > 1$
  - Investor  $i$  observes signal  $s_i = R + \varepsilon_i$

$R \sim N(\bar{R}, 1/\alpha)$  is return of bank's risky asset

$\varepsilon_i \sim N(0, 1/\beta)$  is an iid noise term independent of  $R$

## Model setup (ii)

- Balance sheet of the bank at  $t = 0$

Risky assets →	$A$		$D$	← Wholesale deposits
Reserves (cash) →	$C = \phi D$		$K = \gamma A$	← Capital

where  $\phi$  is a liquidity requirement and  $\gamma$  is a capital requirement

- By balance sheet identity we have

$$(1 - \gamma)A = (1 - \phi)D \rightarrow A = \frac{1 - \phi}{1 - \gamma} \text{ (normalizing } D = 1)$$

# Deposit withdrawals

- Let  $x$  denote the proportion of deposits withdrawn at  $t = 1$
- If  $xR_D \leq \phi$  (withdrawals smaller than cash available)
  - Bank does not have to liquidate risky asset
  - In this case the bank fails if

$$RA + \underbrace{(\phi - xR_D)}_{\uparrow} < (1 - x)R_D$$

Cash remaining until  $t = 2$



# Liquidation costs

- If  $xR_D > \phi$  (withdrawals greater than cash available)
  - Bank sells risky asset at price  $R / (1 + \lambda)$ , with  $\lambda > 0$
  - In this case the bank fails if

$$R \left[ A - \underbrace{\frac{xR_D - \phi}{R / (1 + \lambda)}}_{\substack{\uparrow \\ \text{Assets sold at } t = 1}} \right] < (1 - x)R_D$$

# Bank failure

- Putting together the two previous conditions yields

$$R < \frac{1-\gamma}{1-\phi} \left[ R_D - \phi + \lambda \max \{ xR_D - \phi, 0 \} \right] = R^*$$

where  $R^*$  is the bankruptcy point

## Investors' withdrawal decisions (i)

- Let  $p(s_i, x)$  denote probability of bank failure conditional on
  - Signal  $s_i$  of investor  $i$
  - Withdrawal decisions of all other investors described by  $x$
- Simple behavioral rule for investor  $i$

$$\text{Withdraw when } p(s_i, x) > \hat{p}$$

- $\hat{p}$  is an exogenous parameter
- Could be rationalized in terms of delegation to managers

## Investors' withdrawal decisions (ii)

- Clearly  $p(s_i, x)$  should be decreasing in signal  $s_i = R + \varepsilon_i$   
→ Suppose that all investors follow a threshold strategy

Withdraw when  $s_i < s^*$

- Threshold  $s^*$  is determined jointly with bankruptcy point  $R^*$

# Equilibrium

**Proposition:** When the precision  $\beta$  of the investors' signal is large, there is a unique equilibrium characterized by solution to

→ Investor's indifference condition

→ Bankruptcy point

# Comparative statics

- Effect of capital requirements
  - An increase in  $\gamma$  always reduces  $R^*$
  - Makes the bank safer
- Effect of liquidity requirements
  - An increase in  $\phi$  reduces  $R^*$  when  $R^* < 2(1 - \gamma)$
  - Only when the bank is sufficiently safe
  - In the case of risky banks, they become riskier

# Discussion

- Liquidity requirements as a double-edged sword (König, 2015)
- Two effects
  - *Liquidity effect*: larger buffer to withstand shocks
  - *Solvency effect*: lower asset returns

# References

- König, P. (2015), “Liquidity Requirements: A Double-Edged Sword,” *International Journal of Central Banking*.
- Rochet, J.-C., and X. Vives (2004), “Coordination Failures and the Lender of Last Resort,” *Journal of the European Economic Association*.